# Chemistry 3830 

Periodic Table
and
Atomic Structure

## Periodic Table of the Elements

Group


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Main group
Transition Metals
Lanthanides and Actanides
s block p block
d block
f block

## Periodic Table of the Elements

| Group | 1 | 2 |  | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Period |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1 | $\begin{aligned} & 1 \\ & \mathrm{H} \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 2 He |
| 2 | $\begin{gathered} 3 \\ \mathrm{Li} \end{gathered}$ | $\begin{gathered} 4^{4} \\ \mathrm{Be} \end{gathered}$ |  |  |  |  |  |  |  |  |  |  |  | S | $\begin{gathered} 6 \\ \mathrm{C} \end{gathered}$ | $\begin{aligned} & 7 \\ & \mathrm{~N} \end{aligned}$ | $\begin{aligned} & 8 \\ & 0 \end{aligned}$ | $\begin{aligned} & 9 \\ & \mathrm{~F} \end{aligned}$ | $\begin{aligned} & 10 \\ & \mathrm{Ne} \end{aligned}$ |
| 3 | $\begin{aligned} & 11 \\ & \mathrm{Na} \end{aligned}$ | $\begin{gathered} 12 \\ \mathrm{Mg} \end{gathered}$ |  |  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & 13 \\ & \mathrm{Al} \end{aligned}$ | $\begin{aligned} & 14 \\ & \mathrm{Si} \end{aligned}$ | $\begin{gathered} 15 \\ \mathrm{P} \end{gathered}$ | $\begin{gathered} 16 \\ \mathrm{~S} \end{gathered}$ | $\begin{aligned} & 17 \\ & \mathrm{Cl} \end{aligned}$ | $\begin{aligned} & 18 \\ & \mathrm{Ar} \end{aligned}$ |
| 4 | $\begin{aligned} & 19 \\ & \mathrm{~K} \end{aligned}$ | $\begin{aligned} & 20 \\ & \mathrm{Ca} \end{aligned}$ |  | 21 Sc | $\frac{22}{\mathrm{Ti}}$ | $\begin{aligned} & 23 \\ & \mathrm{~V} \end{aligned}$ | $\begin{aligned} & 24 \\ & \mathrm{Cr} \end{aligned}$ | $\begin{gathered} 25 \\ \mathrm{Mn} \end{gathered}$ | $\begin{aligned} & 26 \\ & \mathrm{Fe} \end{aligned}$ | $\begin{aligned} & 27 \\ & \mathrm{Co} \end{aligned}$ | $\begin{aligned} & 28 \\ & \mathrm{Ni} \end{aligned}$ | $\begin{aligned} & 29 \\ & \mathrm{Cu} \end{aligned}$ | $\begin{aligned} & 30 \\ & \mathrm{Zn} \end{aligned}$ | $\begin{array}{r} 31 \\ \mathrm{Ga} \end{array}$ | $\begin{aligned} & 32 \\ & \mathrm{Ge} \end{aligned}$ | $\begin{aligned} & 33 \\ & \mathrm{As} \end{aligned}$ | $\begin{aligned} & 34 \\ & \mathrm{Se} \end{aligned}$ | $\begin{aligned} & 35 \\ & \mathrm{Br} \end{aligned}$ | $\begin{aligned} & 36 \\ & \mathrm{Kr} \end{aligned}$ |
| 5 | $\begin{aligned} & 37 \\ & \mathrm{Rb} \end{aligned}$ | $\begin{aligned} & 38 \\ & \mathrm{Sr} \end{aligned}$ |  | $\begin{aligned} & 39 \\ & Y \end{aligned}$ | $\begin{aligned} & 40 \\ & \mathrm{Zr} \end{aligned}$ | $\begin{aligned} & 41 \\ & \mathrm{Nb} \end{aligned}$ | $\begin{aligned} & 42 \\ & \text { Mo } \end{aligned}$ | $\begin{aligned} & 43 \\ & \mathrm{Tc} \end{aligned}$ | $\begin{aligned} & 44 \\ & \mathrm{Ru} \end{aligned}$ | $\begin{aligned} & 45 \\ & \text { Rh } \end{aligned}$ | $\begin{aligned} & 46 \\ & \mathrm{Pd} \end{aligned}$ | $\begin{gathered} 47 \\ \mathrm{Ag} \end{gathered}$ | $\begin{aligned} & 48 \\ & \mathrm{Cd} \end{aligned}$ | $\begin{aligned} & 49 \\ & \text { In } \end{aligned}$ | $\begin{aligned} & 50 \\ & \mathrm{Sn} \end{aligned}$ | $\begin{aligned} & 51 \\ & S b \end{aligned}$ | $\begin{aligned} & 52 \\ & \mathrm{Te} \end{aligned}$ | $\begin{gathered} 53 \\ \mathrm{I} \end{gathered}$ | $\begin{array}{r} 54 \\ \mathrm{Xe} \end{array}$ |
| 6 | $\begin{aligned} & 55 \\ & \mathrm{Cs} \end{aligned}$ | $\begin{aligned} & 56 \\ & \mathrm{Ba} \end{aligned}$ | * | $\begin{aligned} & 71 \\ & \mathrm{Lu} \end{aligned}$ | $\begin{aligned} & 72 \\ & \mathrm{Hf} \end{aligned}$ | $\begin{aligned} & 73 \\ & \mathrm{Ta} \end{aligned}$ | $\begin{aligned} & 74 \\ & \mathrm{~W} \end{aligned}$ | $\begin{aligned} & 75 \\ & \operatorname{Re} \end{aligned}$ | $\begin{aligned} & 76 \\ & \text { Os } \end{aligned}$ | $\begin{aligned} & 77 \\ & \mathrm{Ir} \end{aligned}$ | $\begin{aligned} & 78 \\ & \mathrm{Pt} \end{aligned}$ | $\begin{gathered} 79 \\ \mathrm{Au} \end{gathered}$ | $\begin{gathered} 80 \\ \mathrm{Hg} \end{gathered}$ | $\begin{aligned} & 8_{1} \\ & \mathrm{Tl} \end{aligned}$ | $\begin{aligned} & 82 \\ & \mathrm{~Pb} \end{aligned}$ | $\begin{aligned} & 83 \\ & \mathrm{Bi} \end{aligned}$ | $\begin{aligned} & 84 \\ & \mathrm{P}_{0} \end{aligned}$ | $\begin{aligned} & 85 \\ & \text { At } \end{aligned}$ | $\begin{aligned} & 86 \\ & R n \end{aligned}$ |
| 7 | $\begin{aligned} & 87 \\ & \mathrm{Fr} \end{aligned}$ | $\begin{aligned} & \text { 8s } \\ & \text { Ra } \end{aligned}$ | ** | $\begin{aligned} & 103 \\ & \mathrm{Lr} \end{aligned}$ | $\begin{aligned} & 104 \\ & R f \end{aligned}$ | $\begin{aligned} & 105 \\ & \mathrm{Db} \end{aligned}$ | $\begin{aligned} & 106 \\ & \mathrm{Sg} \end{aligned}$ | $\begin{aligned} & 107 \\ & \mathrm{Bh} \end{aligned}$ | $\begin{aligned} & 108 \\ & \mathrm{Hs} \end{aligned}$ | $\begin{aligned} & 109 \\ & \mathrm{Mt} \end{aligned}$ | $\begin{aligned} & { }^{110} \\ & \text { Ds } \end{aligned}$ | $\begin{aligned} & 111 \\ & \mathrm{Rg} \end{aligned}$ | $\begin{gathered} 112 \\ \text { Uub } \end{gathered}$ | $\begin{aligned} & 113 \\ & \text { Uut } \end{aligned}$ | $\begin{aligned} & 114 \\ & \text { Uuq } \end{aligned}$ | $\begin{gathered} 115 \\ \text { Uup } \end{gathered}$ | $\begin{gathered} 116 \\ \text { Uuh } \end{gathered}$ | $\begin{gathered} 117 \\ \text { Uus } \end{gathered}$ | $\begin{gathered} 118 \\ \text { Uuo } \end{gathered}$ |
| s-block |  |  | d-block p-block |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| *Lanthanides | * | 57 La | S8 Ce | 59 Pr | $\begin{aligned} & 60 \\ & \mathrm{Nd} \end{aligned}$ | $\begin{gathered} 61 \\ \mathrm{Pm} \end{gathered}$ | $\begin{gathered} 62 \\ \mathrm{Sm} \end{gathered}$ | $\begin{aligned} & 63 \\ & \mathrm{Eu} \end{aligned}$ | $\begin{gathered} 64 \\ \text { Gd } \end{gathered}$ | $\begin{aligned} & 65 \\ & \text { Tb } \end{aligned}$ | $\begin{aligned} & 66 \\ & \text { Dy } \end{aligned}$ | $\begin{aligned} & 67 \\ & \mathrm{Ho} \end{aligned}$ | $\begin{aligned} & 68 \\ & \mathrm{Er} \end{aligned}$ | $\begin{gathered} 69 \\ T m \end{gathered}$ | $\begin{aligned} & 70 \\ & \mathrm{Yb} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| **Actinides | ** | $\begin{aligned} & 89 \\ & \mathrm{Ac} \end{aligned}$ | $\begin{aligned} & 90 \\ & \text { Th } \end{aligned}$ | $\begin{aligned} & 91 \\ & \mathrm{~Pa} \end{aligned}$ | $\begin{gathered} 92 \\ \mathrm{U} \end{gathered}$ | $\begin{aligned} & 93 \\ & \mathrm{~Np} \end{aligned}$ | 94 Pu | $\begin{gathered} 95 \\ \text { Am } \end{gathered}$ | Cm | $\begin{aligned} & 97 \\ & \mathrm{Bk} \end{aligned}$ | Cf | 99 Es | 100 Fm | $\begin{aligned} & 101 \\ & \mathrm{Md} \end{aligned}$ | $\begin{aligned} & 102 \\ & \text { No } \end{aligned}$ |

f-block

## Three Different Periodic Tables



## Three Different Periodic Tables



| *Lanthanides + 1 | * | La | $\begin{array}{r} 58 \\ \mathrm{Ce} \end{array}$ | $\begin{aligned} & 59 \\ & \mathrm{Pr} \end{aligned}$ | $\begin{aligned} & 60 \\ & \mathrm{Nd} \end{aligned}$ | $\begin{array}{r} 61 \\ \text { Pm } \end{array}$ | $\begin{gathered} 62 \\ 5 m \end{gathered}$ | $\begin{aligned} & 63 \\ & \mathrm{Eu} \end{aligned}$ | $\begin{aligned} & 64 \\ & \text { Gd } \end{aligned}$ | $\begin{aligned} & 65 \\ & \mathrm{~Tb} \end{aligned}$ | $\begin{aligned} & 66 \\ & \text { Dy } \end{aligned}$ | $\begin{aligned} & 67 \\ & \mathrm{Ho} \end{aligned}$ | $\begin{aligned} & 68 \\ & \mathrm{Er} \end{aligned}$ | $\begin{aligned} & { }^{69} \\ & \mathrm{Tm} \end{aligned}$ | $\begin{aligned} & 70 \\ & \mathrm{Yb} \end{aligned}$ | $\begin{aligned} & \text { 71 } \\ & \mathrm{Lu} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| **Actinides + 1 | ** | $\begin{aligned} & B 9 \\ & \text { Ac } \end{aligned}$ | $\begin{aligned} & 90 \\ & \text { Th } \end{aligned}$ | $\begin{aligned} & 91 \\ & \mathrm{~Pa} \end{aligned}$ | $\begin{aligned} & 92 \\ & U \end{aligned}$ | $\begin{aligned} & 93 \\ & \mathrm{~Np} \end{aligned}$ | $\begin{aligned} & 94 \\ & \mathrm{Pu} \end{aligned}$ | $\begin{gathered} 95 \\ \text { Am } \end{gathered}$ | $\begin{gathered} 96 \\ \mathrm{Cm} \end{gathered}$ | $\begin{aligned} & 97 \\ & \text { Bk } \end{aligned}$ | $\begin{aligned} & 98 \\ & \mathrm{Cf} \end{aligned}$ | $\begin{aligned} & 99 \\ & \text { Es } \end{aligned}$ | $\begin{aligned} & 100 \\ & \mathrm{Fm} \end{aligned}$ | $\begin{aligned} & 101 \\ & \mathrm{Md} \end{aligned}$ | $\begin{aligned} & 102 \\ & \text { No } \end{aligned}$ | 103 |

## Introduction to $d$ and $f$-Block Chemistry

Abundances of the elements in the earth's crust:

| \% abundance | elements |
| :--- | :--- |
| $>10$ | $\mathrm{O}, \mathrm{Si}$ |
| $10^{-1}$ | $\mathrm{Al}, \mathrm{Fe}, \mathrm{Ca}, \mathrm{Na}, \mathrm{K}, \mathrm{Mg}$ |
| $1-10^{-1}$ | $\mathrm{H}, \mathrm{Ti}, \mathrm{Cl}, \mathrm{P}$ |
| $10^{-1}-10^{-2}$ | $\mathrm{Mn}, \mathrm{F}, \mathrm{Ba}, \mathrm{Sr}, \mathrm{S}, \mathrm{C}, \mathrm{N}, \mathrm{Zr}, \mathrm{V}, \mathrm{Cr}$ |
| $10^{-2}-10^{-3}$ | $\mathrm{Rb}, \mathrm{Ni}, \mathrm{Zn}, \mathrm{Ce}, \mathrm{Cu}, \mathrm{Y}, \mathrm{La}, \mathrm{Nd}, \mathrm{Co}, \mathrm{Sc}, \mathrm{Li}, \mathrm{Nb}, \mathrm{Ga}, \mathrm{Pb}, \mathrm{Th}, \mathrm{B}$ |
| $10^{-3}-10^{-4}$ | $\mathrm{Pr}, \mathrm{Br}, \mathrm{Sm}, \mathrm{Gd}, \mathrm{Ar}, \mathrm{Yb}, \mathrm{Cs}, \mathrm{Dy}, \mathrm{Hf}, \mathrm{Er}, \mathrm{Be}, \mathrm{Xe}, \mathrm{Ta}, \mathrm{Sn}, \mathrm{U}, \mathrm{As}, \mathrm{W}, \mathrm{Mo}, \mathrm{Ge}, \mathrm{Ho}, \mathrm{Eu}$ |
| $10^{-4}-10^{-5}$ | $\mathrm{~Tb}, \mathrm{I}, \mathrm{TI}, \mathrm{Tm}, \mathrm{Lu}, \mathrm{Sb}, \mathrm{Cd}, \mathrm{Bi}, \mathrm{In}$ |
| $10^{-5}-10^{-6}$ | $\mathrm{Hg}, \mathrm{Ag}, \mathrm{Se}, \mathrm{Ru}, \mathrm{Te}, \mathrm{Pd}, \mathrm{Pt}$ |
| $10^{-6}-10^{-7}$ | $\mathrm{Rh}, \mathrm{Os}, \mathrm{Ne}, \mathrm{He}, \mathrm{Au}, \mathrm{Re}, \mathrm{Ir}$ |
| $10^{-7}-10^{-9}$ | Kr |
| $10^{-9}-10^{-20}$ | $\mathrm{Ra}, \mathrm{Pa}, \mathrm{Ac}, \mathrm{Po}, \mathrm{Rn}, \mathrm{Np}, \mathrm{Pu}, \mathrm{Pm}$ |
| $<10^{-20}$ | $\mathrm{Fr}, \mathrm{At}, \mathrm{transplutonium} \mathrm{elements}$ |

Blue = 1st row TM, Red = 2nd row TM, Green = 3rd row TM

- In general, $1^{\text {st }}$ row TMs are more abundant than $2^{\text {nd }}$ or $3^{\text {rd }}$ row TMs.


## Introduction to $d$ and $f$-Block Chemistry

## Mineral sources and methods of recovery for some commercially important d-block metals:

| Metal | Principal minerals | Method of recovery |
| :---: | :---: | :---: |
| Titanium | Ilmenite, $\mathrm{FeTiO}_{3}$ Rutile, $\mathrm{TiO}_{2}$ | $\mathrm{TiO}_{2}+2 \mathrm{C}+2 \mathrm{Cl}_{2} \rightarrow \mathrm{TiCl}_{4}+2 \mathrm{CO}$ <br> followed by reduction of $\mathrm{TiCl}_{4}$ with Na or Mg |
| Vanadium | Vanadinite, $\mathrm{Pb}_{5}\left(\mathrm{VO}_{4}\right)_{3} \mathrm{Cl}$ |  |
| Chromium | Chromite, $\mathrm{FeCr}_{2} \mathrm{O}_{4}$ | $\mathrm{FeCr}_{2} \mathrm{O}_{4}+4 \mathrm{C} \rightarrow \mathrm{Fe}+2 \mathrm{Cr}+4 \mathrm{CO}$ |
| Molybdenum | Molybdenite, $\mathrm{MoS}_{2}$ | $2 \mathrm{MoS}_{2}+7 \mathrm{O}_{2} \rightarrow 2 \mathrm{MoO}_{3}+4 \mathrm{SO}_{2}$ <br> followed by either: <br> $\mathrm{MoO}_{3}+2 \mathrm{Fe} \rightarrow \mathrm{Mo}+\mathrm{Fe}_{2} \mathrm{O}_{3}$ or $\mathrm{MoO}_{3}+3 \mathrm{H}_{2} \rightarrow \mathrm{Mo}+3 \mathrm{H}_{2} \mathrm{O}$ |
| Tungsten | Scheelite, $\mathrm{CaWO}_{4}$ Wolfamite, $\mathrm{FeMn}\left(\mathrm{WO}_{4}\right)_{2}$ | $\begin{aligned} & \mathrm{CaWO}_{4}+2 \mathrm{HCl} \rightarrow \mathrm{WO}_{3}+\mathrm{CaCl}_{2}+\mathrm{H}_{2} \mathrm{O} \\ & \text { followed by } 2 \mathrm{WO}_{3}+6 \mathrm{H}_{2} \rightarrow 2 \mathrm{~W}+6 \mathrm{H}_{2} \mathrm{O} \end{aligned}$ |
| Manganese | Pyrolusite, $\mathrm{MnO}_{2}$ | $\mathrm{MnO}_{2}+\mathrm{C} \rightarrow \mathrm{Mn}+\mathrm{CO}_{2}$ |
| Iron | Hematite, $\mathrm{Fe}_{2} \mathrm{O}_{3}$ <br> Magnetite, $\mathrm{Fe}_{3} \mathrm{O}_{4}$ <br> Limonite, $\mathrm{FeO}(\mathrm{OH})$ | $\mathrm{Fe}_{2} \mathrm{O}_{3}+3 \mathrm{CO} \rightarrow 2 \mathrm{Fe}+3 \mathrm{CO}_{2}$ |
| Cobalt | Cobaltite, CoAsS <br> Smaltite, $\mathrm{CoAs}_{2}$ <br> Linnaeite, $\mathrm{Co}_{3} \mathrm{~S}_{4}$ | byproduct of copper and nickel production |
| Nickel | Pentlandite, $(\mathrm{Fe}, \mathrm{Ni})_{6} \mathrm{~S}_{8}$ | $2 \mathrm{NiS}+2 \mathrm{O}_{2} \rightarrow 2 \mathrm{Ni}+2 \mathrm{SO}_{2}$ |
| Copper | Chalcopyrite, $\mathrm{CuFeS}_{2}$ Chalcocite, $\mathrm{Cu}_{2} \mathrm{~S}$ | $2 \mathrm{CuFeS}_{2}+2 \mathrm{SiO}_{2}+5 \mathrm{O}_{2} \rightarrow 2 \mathrm{Cu}+2 \mathrm{FeSiO}_{3}+4 \mathrm{SO}_{2}$ |

- Oxides preferred for $1^{\text {st }}$ row and early TMs
- Sulfides preferred for $2^{\text {nd }} / 3^{\text {rd }}$ row and late TMs


## Atomic Structure

Atoms consist of
(i) a nucleus (containing protons and neutrons)
(ii) Electron shell
(i) Nucleus:

Positively charged (because of protons)
Very small, $10^{-15} \mathrm{~m}=1 \mathrm{fm}$
Number of protons define the element
(ii) Electron shell:

Planetary Model


Negatively charged (because of electrons)
Electron shell will define the size of the atom $\left(10^{-10} \mathrm{~m}=100 \mathrm{pm}=1 \AA\right.$ )
Electrons are extremely small (estimated as $10^{-18} \mathrm{~m}$ )
Atoms are mainly empty space!
In chemistry (NOT nuclear chemistry), only electrons are involved in chemical reactions

## Electronic Structure of an Atom

How can we study the electronic structure of the atom?
Answer: Through interaction of electromagnetic radiation with matter!

What is electromagnetic radiation?

Electric and magnetic components (mathematical description: Maxwell's equations)

## Electromagnetic radiation



## Wave Particle Duality of Electromagnetic Radiation

Wavelength and frequency

c = speed of light in the vacuum
$=2.997925 \times 10^{8} \mathrm{~m} / \mathrm{s}$

Diffraction experiment for example: X-ray crystallography

Photon of a particular energy

Energy of a photon: $E=h v$
$\mathrm{h}=$ Planck's constant
$=6.62607 \times 10^{-34} \mathrm{Js}$

Photoelectric effect (Einstein)

Absorption and emission spectra

## Bohr Model of the Atom

Two postulates:
(i) In the absence of radiation absorption or emission, electrons stay in a stationary state.
(ii) Absorption occurs only in discrete amounts, corresponding to a change in energy between two stationary states of the electron.

Electronic energies are quantized ( $\mathrm{n}=$ principle quantum number)

Energy of an electron in the state n :

$$
\begin{aligned}
& E_{n}=-\frac{m_{e} e^{4}}{8 \varepsilon_{0}^{2} h^{2}}\left(\frac{Z^{2}}{n^{2}}\right)=-R_{H}\left(\frac{Z^{2}}{n^{2}}\right) R_{H}=2.149 \times 10^{-18} \mathrm{~J} \\
& \left|E_{n}-E_{m}\right|=h v=\frac{Z^{2} m_{e} e^{4}}{8 \varepsilon_{0}^{2} h^{2}}\left(\frac{1}{n_{n}^{2}}-\frac{1}{n_{m}^{2}}\right)
\end{aligned}
$$

## Bohr Model of the Atom

$$
r_{n}=\frac{\varepsilon_{0} h^{2}}{Z \pi m e^{2}} n^{2}=a_{0} \frac{n^{2}}{Z} ; Q_{0}=\text { Bohr radius }=52.9 \mathrm{pm}
$$



## Wave Particle Duality of Subatomic Particles

particle

wave

Electrons, protons, neutrons
?

Certain mass and size

Diffraction experiment for example: neutron or electron diffraction

## De Broglie equation



Wavelength of electrons
(and neutrons, protons and any matter)

## Diffraction Experiment

Light can be diffracted using a grid or a lattice (crystal lattice in X-ray crystallography) A diffraction experiment is using the wave description.

Particles (neutrons and electrons) can be diffracted.


Electron diffraction through a sheet of crystalline aluminium (historic experiment)

## The Schröderinger Wave Equation

$$
\widehat{H} \Psi=E \Psi
$$

Wavefunction
Hamiltonian (operator) Energy

$$
\hat{A} \Psi=c \Psi
$$

Operator
Eigenvalue
Wavefunction (Eigenfunction)

## Electronic Wavefunctions?

We want to know the electronic wavefunctions

$$
\widehat{H} \Psi=E \Psi
$$

We can describe the Hamiltonian (energy) operator

Kinetic energy of nucleus Kinetic energy of electron

Potential energy: Electron-nucleus attraction


We need to "solve Schrödinger's equation" to get the allowed wavefunctions

## Spherical Polar Coordinate System



## Spherical polar coordinates

$r$ is the radius<br>$\theta$ is the colatitude<br>$\phi$ is the azimuth

In this coordinate system, the equation describing a spherical surface is simply $f(r, \theta, \phi)=r$
i.e., if $r=3$, a sphere of radius 3

## Solving Schröderinger's Equation

$$
\widehat{H} \Psi=E \Psi
$$

1. Conversion from Cartesian Coordinates (xyz) to

Spherical Polar Coordinates (r, $\theta$ \{theta\}, $\varphi\{p h i\}$ )
2. Separation of variables, three different subfunctions:

$$
\Psi=R(r) \Theta(\theta) \Phi(\varphi)
$$

"solving Schrödinger's equation"

$$
\begin{gathered}
\frac{1}{\mathrm{R}} \frac{d}{d r}\left(r^{2} \frac{d R}{d r}\right)+\frac{8 \pi^{2} m}{h^{2}}+\left(E+\frac{Z e^{2}}{4 \pi \varepsilon_{0} r}\right) r^{2}=\mathrm{u} \text { ( } R \text { subfunction) } \\
\frac{1}{\sin \theta} \frac{d}{d \theta}\left(\sin \theta \frac{d \Theta}{d \theta}\right)-\frac{v^{2}}{\sin ^{2} \theta}+u \Theta=0(\Theta \text { subfunction }) \\
\frac{1}{\Phi} \frac{d^{2}}{d \varphi^{2}}=-v^{2}(\Phi \text { subfunction })
\end{gathered}
$$

Quantum numbers: $u=1(1+1) ; v=m_{1}$

## Solving Schröderinger's Equation

$$
\begin{gathered}
\widehat{H} \Psi=E \Psi \\
\Psi=R(r) \Theta(\theta) \Phi(\varphi)=R(r) Y(\theta, \varphi) \\
\text { radial wavefunction angular wavefunction }
\end{gathered}
$$



Only certain wavefunctions are allowed! Only certain quantum numbers are allowed!

## Quantum Numbers

$\mathrm{n}=$ principle quantum number (information about the shell, information about energy) $n=1,2,3,4, \ldots \ldots$

## Quantum Numbers

$$
\begin{aligned}
& 1=\underline{\text { angular momentum quantum number }} \\
& \begin{array}{l}
\text { (information about the subshell, } \\
\text { type of orbital, }
\end{array} \\
& 1=0,1,2,3, \ldots .(\mathrm{n}-1)
\end{aligned}
$$

angular momentum of an electron in an orbital: $\quad \hat{L}^{2} \Psi=l(l+1) \hbar^{2} \Psi$

$$
|L|=\sqrt{l(l+1)} \hbar
$$

| Orbital names assigned to values of $l$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $l$ | 0 | 1 | 2 | 3 | 4 | 5 |
| orbital label | $s$ | $p$ | $d$ | $f$ | g | $h$ |

## Quantum Numbers

$\mathrm{m}_{1}=\underline{\text { magnetic quantum number (information about the orientation of the orbital, }}$ or the z-component of the angular momentum)
$m_{1}=0, \pm 1, \pm 2, \pm 3, \ldots . \pm 1$
z-component of the angular momentum of an orbital: $\quad \hat{L}_{z} \Psi=m_{l} \hbar \Psi$

$$
\Psi=R_{n, l}(r) Y_{l, m_{l}}(\theta, \varphi)
$$

## Quantum Numbers

$\mathrm{m}_{\mathrm{s}}=\underline{\text { electron } \text { spin quantum number }}$
Orbitals defined by the quantum numbers n , I and $\mathrm{m}_{1}$ may contain up to two electrons

Each of the electrons has a unique "electron spin" and is usually denoted as "spin up" $\uparrow$ and "spin down" $\downarrow$
$\mathrm{m}_{\mathrm{s}}=+1 / 2,-1 / 2$

